## Readers' Forum

Brief discussions of previous investigations in the aerospace sciences and technical comments on papers published in the AIAA Journal are presented in this special department. Entries must be restricted to a maximum of 1000 words, or the equivalent of one Journal page including formulas and figures. A discussion will be published as quickly as possible after receipt of the manuscript. Neither the AIAA nor its editors are responsible for the opinions expressed by the correspondents. Authors will be invited to reply promptly.

## Comment on "A New Solution Method for Lifting Surfaces in Subsonic Flow"

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THIS commentator objects to the characterization by Ueda and Dowell<sup>1</sup> of the principal approximation of the Doublet-Lattice Method (DLM)<sup>2</sup> as inconsistent while the "new solution" contains actual inconsistencies. The principal approximation was clearly stated in the original paper (Ref. 2, p. 281): "In order to converge to Hedman's vortex-lattice results for steady flow and to improve the approximation of Eq. (7), the authors have found it necessary to subtract the steady part ( $\omega = 0$ ) from  $\Re$  before applying the preceding formulas, and then to add the effect of a horseshoe vortex.' This made the DLM consistent with the Vortex-Lattice Method (VLM) of Hedman<sup>3</sup> (and also of Rubbert, 4 Dulmovits,<sup>5</sup> and Belotserkovskii<sup>6</sup>). It is Ueda and Dowell who are inconsistent in the limit of zero frequency with the accepted formulation of the VLM<sup>7</sup> which is characterized by swept bound vortices on a swept planform. The characterization of their method is also inconsistent: their Doublet Point Method (DPM) is not a point method at all, but is a rectangular DLM in which the doublet line is not swept. The tradeoff that has been made is between the rectangular geometry that permits exact spanwise integration of the kernel and the swept geometry of the bound leg in the DLM with its necessary approximations.

A comparison of the DPM and DLM on swept planforms should have been the subject of the Numerical Results section of Ref. 1, but, instead the comparisons are primarily with the pressure loading function (kernel-function) methods of Laschka<sup>8</sup> and Rowe.<sup>9</sup> These comparisons hardly demonstrate any advantage of the DPM over the DLM! A meaningful comparison with the effects of variable sweep could have been made with the circular wing for which an exact solution exists.10 The circular wing was a standard problem in the AGARD SMP study of isolated surfaces and the DLM results are included in the summary report of Woodcock.11 Even when a comparison of the two methods could have been made with the experimental data of Försching et al., 12 the opportunity was missed: Petkas' version of the DLM13 was correlated with Försching's control surface data in Figs. 2 and 3 of Ref. 14 (which is Ref. 10 of Ueda and Dowell!).

Another inconsistency in Ref. 1 is the use of an undefined dimensional reduced frequency, presumably the angular frequency divided by the freestream velocity. The accuracy of results for a reduced frequency k=1 and 5 chordwise elements is questionable inasmuch as a sufficient number of lifting elements per wave length may not have been used.

Reference 1 also does not discuss the nonplanar problem. It

is not likely that the nonplanar kernels<sup>15,16</sup> can be integrated in closed form even with the rectangular simplifications, so this leaves us with one more "new solution" to the *isolated* lifting surface problem. The DLM was motivated by the T-tail flutter problem<sup>17</sup> (the T-tail was an example in the original paper<sup>2</sup>), and the DLM now provides a solution for subsonic wing-body interference. <sup>18</sup> The DPM does not appear to offer comparable growth potential.

## References

<sup>1</sup>Ueda, T. and Dowell, E. H., "A New Solution Method for Lifting Surfaces in Subsonic Flow," *AIAA Journal*, Vol. 20, March 1982, pp. 348-355.

1982, pp. 348-355.

<sup>2</sup>Albano, E., and Rodden, W. P., "A Doublet-Lattice Method for Calculating Lift Distributions on Oscillating Surfaces in Subsonic Flows," *AIAA Journal*, Vol. 7, Feb. 1969, pp. 279-285, "Errata," Nov. 1969, p. 2192.

<sup>3</sup>Hedman, S. G., "Vortex Lattice Method for Calculation of Quasi Steady State Loadings on Thin Elastic Wings," Aeronautical Research Institute of Sweden, Rept. 105, Oct. 1965.

<sup>4</sup>Rubbert, P. E., "Theoretical Characteristics of Arbitrary Wings by a Nonplanar Vortex Lattice Method," The Boeing Company, Seattle, Wash., Rept. D6-9244, 1965.

<sup>5</sup>Dulmovits, J., "A Lifting Surface Method for Calculating Load Distributions and the Aerodynamic Influence Coefficient Matrix for Wings in Subsonic Flow," Grumman Aircraft Engineering Corp., Bethpage, N.Y., Rept. ADR 01-02-64.1, 1964.

<sup>6</sup>Belotserkovskii, S. M., *The Theory of Thin Wings in Subsonic Flow*, Plenum Press, New York, 1967.

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<sup>8</sup>Laschka, B., "Zur Theorie der harmonisch schwingenden tragenden Flache bei Unterschallanstromung," Zeitschrift für Flugwissenschaften, Heft 7, 1963, pp. 265-291.

<sup>9</sup>Rowe, W. S., Redman, M. C., Ehlers, F. E., and Sebastian, J. D., "Prediction of Unsteady Aerodynamic Loadings Caused by Leading Edge and Trailing Edge Control Surface Motion in Subsonic Compressible Flow—Analysis and Results," NASA CR-2543, 1975.

<sup>10</sup> Schade, T. and Krienes, K., "The Oscillating Circular Airfoil on the Basis of Potential Theory," NACA TM 1098, 1947.

<sup>11</sup>Woodcock, D. L., "A Comparison of Methods Used in Lifting Surface Theory," AGARD Rept. No. 583, Supplement to the AGARD Manual on Aeroelasticity, Part VI, 1971.

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<sup>12</sup> Försching, H., Triebstein, H., and Wagener, J., "Pressure Measurements on an Harmonically Oscillating Swept Wing with Two Control Surfaces in Incompressible Flow," Symposium on Unsteady Aerodynamics for Aeroelastic Analyses of Interfering Surfaces, AGARD-CP-80-71, Pt. 11, 1971, pp. 15-1-15-12.

<sup>13</sup> Petkas, J. S., "Oscillatory Aerodynamic Representation Using Discrete Load Line Element (DLLE) Method," Lockheed-Georgia Co., Marietta, Ga., unpublished Memorandum, Feb. 1969.

<sup>14</sup>Ashley, H. and Rodden, W. P., "Wing-Body Aerodynamic Interaction," *Annual Review of Fluid Mechanics*, Vol. 4, 1972, pp. 431-472.

431-472.

15 Landahl, M. T., "Kernel Function for Nonplanar Oscillating Surfaces in a Subsonic Flow," *AIAA Journal*, Vol. 5, May 1967, pp. 1045-1046.

<sup>16</sup>Rodden, W. P., Giesing, J. P., and Kálmán, T. P., "Refinement of the Nonplanar Aspects of the Subsonic Doublet-Lattice Lifting Surface Method," *Journal of Aircraft*, Vol. 9, Jan. 1972, pp. 69-73.

<sup>17</sup>Rodden, W. P., "Comment on 'Effect of Stabilizer Dihedral and Static Lift on T-Tail Flutter'," *Journal of Aircraft*, Vol. 15, July 1978, pp. 447-448.

<sup>18</sup> Giesing, J. P., and Kálmán, T. P., and Rodden, W. P., "Subsonic Steady and Oscillatory Aerodynamics for Multiple Interfering Wings and Bodies," *Journal of Aircraft*, Vol. 9, Oct. 1972, pp. 693-702.

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